



Reg. No. :

--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--

**Question Paper Code : 41320**

B.E./B.Tech. DEGREE EXAMINATION, APRIL/MAY 2018

Fifth Semester

Computer Science and Engineering  
MA 6566 – DISCRETE MATHEMATICS  
(Regulations 2013)

Time : Three Hours

Maximum : 100 Marks

Answer ALL questions

PART – A

(10×2=20 Marks)

1. Define proposition.
2. Give the symbolic form of "Some men are giant".
3. Define Pigeon hole principle.
4. How many permutations can be made out of letter or word 'COMPUTER' ?
5. Show that there does not exist a graph with 5 vertices with degrees 1, 3, 4, 2, 3 respectively.
6. Define Hamiltonian path.
7. Define semi group.
8. Prove that in a group idempotent law is true only for identity element.
9. Let  $A = \{1, 2, 5, 10\}$  with the relation divides. Draw the Hasse diagram.
10. Prove that a lattice with five elements is not a Boolean algebra.

PART – B

(5×16=80 Marks)

11. a) i) Show that  $(7P \wedge (7Q \wedge R) \vee (Q \wedge R) \vee (P \wedge R) \Leftrightarrow R$ , without using truth table. (8)  
ii) Show that using Rule C.P,  $7P \vee Q, 7Q \vee R, R \rightarrow S \Rightarrow P \rightarrow S$  (8)  
(OR)
- b) i) Find the PCNF of  $(P \vee R) \wedge (P \vee 7Q)$  Also find its PDNF, without using truth table. (8)  
ii) Show that  $(\forall x) [P(x) \vee Q(x)] \Rightarrow (\forall x) P(x) \vee (\exists x) Q(x)$ . (8)

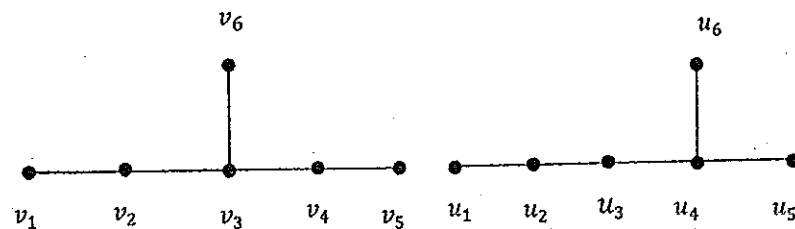


12. a) i) Prove that  $n^3 - n$  is divisible by 3 for  $n \geq 1$  (8)  
 ii) Solve  $G(k) - 7G(k-1) + 10G(k-2) = 8k + 6$ . (8)  
 (OR)

- b) i) Find the numbers between 1 to 250 that are not divisible by any of the integers 2 or 3 or 5 or 7. (8)  
 ii) Solve using generating functions :  $S(n) + 3S(n-1) - 4S(n-2) = 0$ ;  $n \geq 2$  given  $S(0) = 3, S(1) = -2$ . (8)

13. a) i) State and prove Hand shaking theorem. Hence prove that for any simple graph  $G$  with  $n$  vertices, the number of edges of  $G$  is less than or equal to  $\frac{n(n-1)}{2}$ . (8)

- ii) Establish the isomorphism of the following pairs of graphs. (8)



(OR)

- b) i) Prove that a graph  $G$  is disconnected if and only if its vertex set  $V$  can be partitioned into two non-empty, disjoint subsets  $V_1$  and  $V_2$  such that there exists no edge in  $G$  whose one end vertex is in subset  $V_1$  and the other in subset  $V_2$ . (8)  
 ii) Prove that a connected graph  $G$  is an Euler graph if and only if all vertices of  $G$  are of even degree. (8)

14. a) i) Show that  $(\mathbb{Q}^+, *)$  is an abelian group, where  $*$  is defined by  $a * b = \frac{ab}{2}, \forall a, b \in \mathbb{Q}^+$  (8)

- ii) Prove that kernel of a homomorphism is a normal subgroup of  $G$ . (8)

(OR)

- b) i) Prove that intersection of two normal subgroups of a group  $G$  is again a normal subgroup of  $G$ . (8)

- ii) Let  $G$  be a finite group and  $H$  be a subgroup of  $G$ . Then prove that order of  $H$  divides order of  $G$ . (8)



15. a) i) Show that  $(\mathbb{N}, \leq)$  is a partially ordered set, where  $\mathbb{N}$  is the set of all positive integers and  $\leq$  is a relation defined by  $m \leq n$  if and only if  $n - m$  is a non-negative integer. (8)

- ii) In a complemented and distributive lattice, prove that complement of each element is unique. (8)

(OR)

- b) i) Let  $D_{30} = \{1, 2, 3, 5, 6, 10, 15, 30\}$  with a relation  $x \leq y$  if and only if  $x$  divides  $y$ .

Find :

- i) All lower bounds of 10 and 15

- ii) GLB of 10 and 15

- iii) All upper bound are 10 and 15

- iv) LUB of 10 and 15

- v) Draw the Hasse diagram for  $D_{30}$ . (8)

- ii) Let  $(L, \vee, \wedge, \leq)$  be a distributive lattice and  $a, b, c \in L$  if  $a \wedge b = a \wedge c$  and  $a \vee b = a \vee c$ . Then show that  $b = c$ . (8)